$A$ is the centre of circle $C$, with equation $x^{2}-8 x+y^{2}+10 y+1=0$
$P, Q$ and $R$ are points on the circle and the lines $I_{1}, I_{2}$ and $I_{3}$ are tangents to the circle at these points respectively. Line $I_{2}$ intersects line $I_{1}$ at $B$ and line $I_{3}$ at $D$.

Figure 1

a Find the centre and radius of $C$.
b Given that the $x$-coordinate of $Q$ is 10 and that the gradient of $A Q$ is positive, find the $y$-coordinate of $Q$, explaining your solution.
c Find the equation of $I_{2}$, giving your answer in the form $y=m x+b$.
d Given that $A P B Q$ is a square, find the equation of $I_{1}$ in the form $y=m x+b$.
$l_{1}$ intercepts the $y$-axis at $E$.
e Find the area of triangle EPA.

